

A Low Power Error Detection in the Syndrome Calculator Block for Reed-Solomon Codes: RS(204,188)*

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Abstract: Reed-Solomon (RS) codes have been widely adopted in many modern communication systems. This paper describes a new method for error detection in the syndrome calculator block of RS decoders. The main feature of this method is to prove that it is possible to compute only a few syndrome coefficients — less than half — to detect whether the codeword is correct. The theoretical estimate of the probability that the new algorithm failed is shown to depend on the number of syndrome coefficients computed. The algorithm is tested using the RS(204,188) code with the first four coefficients. With a bit error rate of 1×10^{-4} , this method reduces the power consumption by 6% compared to the basic RS(204,188) decoder. The error detection algorithm for the syndrome calculator block does not require modification of the basic hardware implementation of the syndrome coefficients computation. The algorithm significantly reduces the computation complexity of the syndrome calculator block, thus lowering the power needed.

Key words: Reed-Solomon codes; syndrome calculator block; error detection; bit error rate

Introduction

Communication technologies are widely used these days. Due to the growing percentage of people using these technologies, methods are needed to increase the transmission rate without reducing the quality. One of these methods is the Reed-Solomon (RS) codes which are used to correct errors in many systems such as storage devices (CD, DVD, etc.) and digital video broadcasting (DVB).

An RS codeword is a packet of symbols which are commonly bytes (8-bit symbols), denoted as RS(n , k) where n is the number of symbols in the encoded message and k is the number of symbols in the original message. Each RS codeword can correct a maximum

of $t = (n-k)/2$ errors in a received packet.

This work seeks to reduce the number of computations needed for error detection. We prove that it is possible to compute less than half of the syndrome coefficients with quasi-similar error detection reliability. The main parameter of this method is the number of computed syndrome coefficients. The algorithm only computes a few syndrome coefficients. If they are all zero, the codeword is considered to be correct. If the codeword is not correct, the entire syndrome polynomial is obtained so the errors can be corrected through the other blocks^[1]. This paper focuses on proving that this method is reliable by estimating the probability that it fails. The algorithm is also tested and compared to the basic RS decoder.

1 Background and Related Work

The syndrome calculator block provides two results. The first result is whether the received codeword is correct. The second result provides the syndrome

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polynomial which will be used to correct the codeword if the codeword is erroneous. The most common algorithm^[2] to perform the syndrome calculation needs $2t$ basic cells as defined in Fig. 1 with each cell, c_i , giving one syndrome coefficient, S_i , with $1 \leq i \leq 2t$.

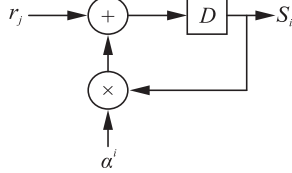


Fig. 1 Basic syndrome calculator cell

In Fig. 1, r_j , $1 \leq j \leq n$, is the j -th coefficient of the received codeword polynomial, $r(x)$, so n computations are needed to compute the syndrome polynomial. All the syndrome coefficients will be equal to 0 if the received codeword is correct with at least one coefficient different from 0 if the codeword is not correct.

Much work has been done to reduce time-consuming computational steps. Costa et al.^[3] developed a new fast Fourier transform (FFT) method based on the cyclotomic FFT to compute the syndrome using a method that corresponds to the partial discrete Fourier transform (DFT) of $D(x)$. This algorithm is better than the Horner rule^[4] and the Zakharova method^[5]. In 2007, Lin et al.^[6] developed a method based on the Trifono-Fedorenko^[7] procedure, showing that the problem of computing the syndromes for time-domain RS decoders can be solved by the use of affine polynomials with a sequence of vectors. Their method has very good results for finite fields.

All these algorithms depend on modifications of the conventional syndrome computational method. Lee et al.^[8] provided a method for reducing the number of computations in syndrome polynomials by decoding error correction codes without modifying the standard method. The relationship between the syndromes and the coefficients of the error locator polynomial^[1] infers that if the first t syndromes are zeros, the next t syndromes must also be zeros. Thus, only half of the syndromes must be calculated to know if the codeword is correct.

2 Theory of the Error Checking Algorithm

Some following notations are defined to simplify the explanation:

- h is the number of zeros in the syndrome vector.
- N_{synd} , $1 \leq N_{\text{synd}} \leq t-1$, corresponds to the number of first coefficients in the syndrome vector. For instance, if $N_{\text{synd}}=4$, the calculation uses S_1, S_2, S_3 , and S_4 .
- P_{zeros} is the probability to have h or N_{synd} verified.

The objective is to show that less than half of the syndromes are needed to check whether the codeword is correct. The only parameter in the algorithm shown in Fig. 2 is N_{synd} .

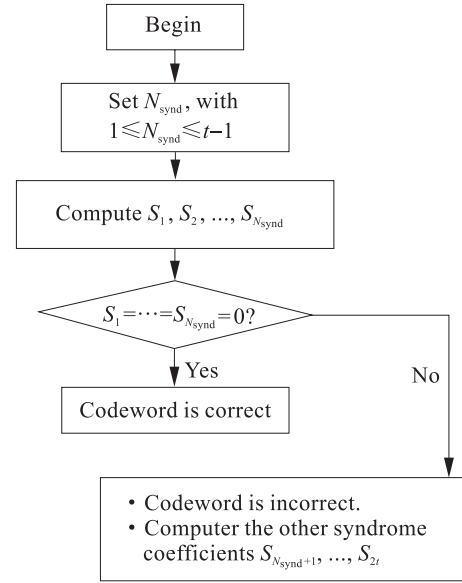


Fig. 2 Error checking algorithm

From the algorithm in Fig. 2,

- For a correct codeword, the algorithm never fails.
- For an erroneous codeword, the algorithm could fail if the few first components, N_{synd} , of the syndrome vector are zero.

The Hamming distance implies that i syndrome coefficients with $i < t$ are able to detect only $i-1$ errors. Therefore, this algorithm could fail in some cases. The following estimates the failure rate:

The RS(n, k) syndrome calculator computes the syndrome vector with R as the received codeword, C the sent codeword, and E the errors in the received codeword.

$$S_{i+1} = R(\alpha^i) = C(\alpha^i) + E(\alpha^i) = E(\alpha^i), \quad 0 \leq i \leq 2t-1 \quad (1)$$

$C(\alpha^i)=0$ according to the definition of the RS codeword, and

$$R(x) = R_0 + R_1x + R_2x^2 + \dots + R_{N-1}x^{N-1} \quad (2)$$

R_{N-1} is the first received symbol.

If the codeword R is correct, the syndrome vector is zero, but if the codeword is erroneous and given by

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