



Prediction of tree diameter growth using quantile regression and mixed-effects models



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ABSTRACT

A tree diameter growth function is an important component of an individual-tree model. This function can be considered as a mixed-effects model, in which a diameter measurement can be used to calibrate (or localize) the equation to produce improved diameter predictions for the same tree in the future. Another approach considered in this study involved a system of quantile regressions, in which future diameters can be determined through interpolation, based on a current diameter measurement. The aim of this study was to evaluate the use of quantile regression and mixed-effects models in predicting tree diameter growth. Tree diameter at the end of each growth period was predicted from diameter at the beginning of the period by use of one of the four methods: the mixed-effects model and three quantile regression methods that were based on nine quantiles, five quantiles, and three quantiles. The mixed-effects model performed as well as the three quantile regression methods, based on the mean absolute difference and fit index, but was far superior in terms of the mean difference. The mixed-effects model produced an unbiased prediction of future diameter, up to ten years into the future, when calibrated with a current diameter measurement.

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1. Introduction

Forest management decisions are often based on current stand conditions, obtained from inventory data, and future stand conditions, predicted from growth and yield models. A tree diameter growth function is an important component of an individual-tree model, which simulates survival and growth of individual trees in a forest stand (Avery and Burkhart, 2002). It can also be incorporated into a stand-table projection system (Cao, 2007), which predicts future movements of trees among diameter classes.

Recently, there has been a growing interest in applying mixed-effects models to solve forestry regression problems, such as predicting timber volume (Hall and Clutter, 2004), dominant height growth (Fang and Bailey, 2001), tree mortality (Groom et al., 2012), and tree taper (Cao and Wang, 2011), to name a few. A mixed-effects diameter growth model can be developed which contains both fixed-effects parameters that are common to all trees in the sample, and random effects that are specific to each tree. When these random effects are calculated by use of measure-

ment(s) from a particular tree, the model is said to be calibrated (or localized) for that tree. Results are improved predictions for future diameters of that tree.

Quantile regression (Koenker and Bassett, 1978) has recently been employed by scientists from various backgrounds to address different kinds of problems. These include research in medicine (Austin and Schull, 2003), economics (Machado and Mata, 2005), education and policy (Haile and Nguyen, 2008), and natural resource management (Cade et al., 2005). In forestry, quantile regression has been applied to model self-thinning boundary lines (Zhang et al., 2005) and tree diameter percentiles (Mehtatalo et al., 2008), compute stand density index (Ducey and Knapp, 2010), or evaluate the spread rate of forest diseases (Evans and Finkral, 2010).

Individual tree growth from a locality might not follow the path modeled by a published tree-level equation, which gives predictions based on average tree growth. It is well known that a tree model can be localized by use of the mixed model approach. We introduce in this paper a new method for local tree-level predictions that involves quantile regression models. These models constitute a set of quantile diameter curves, similar to a set of site index curves, that can be used to predict tree diameter at a future age from past diameter measurement, assuming that the relative

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location of the tree does not change over time. The objective of this paper is to evaluate the use of quantile regression and mixed-effects models in predicting tree diameter growth.

2. Material and methods

2.1. Data

The data set consisted of measurements collected from 340 trees in an unthinned loblolly pine (*Pinus taeda* L.) plantation in Lee Memorial Forest near Bogalusa, Louisiana, USA. The trees were planted in a 2.7 m by 3.7 m spacing. Diameters at breast height were recorded annually from age 2 to age 21 (Fig. 1), totaling 6147 observations.

The data were randomly divided into five groups of 68 trees each (Table 1). The leave-one-out evaluation scheme was applied in this study. The scheme consisted of five stages, each involved validation data from a group and fit data from the remaining four groups. Parameters of the diameter growth model were estimated from the fit data, and then used to predict for the validation data. The predictions from all stages were used to compute evaluation statistics for the different methods.

2.2. Diameter growth model

Several growth functions were investigated in a preliminary analysis. The function that fit the data best had a similar form to that of the height–age function developed by Bailey and Clutter (1974):

$$y(t_{ij}) = \exp(b_1 + b_2 t_{ij}^{b_3}) + \varepsilon_{ij}, \tag{1}$$

where $y(t_{ij})$ is diameter at breast height (cm) of measurement j for tree i at age t_{ij} , and b_k 's are regression parameters.

2.3. Mixed-effects model

In the mixed-effects framework, all parameters of Eq. (1) can be expressed as fixed-effects parameters (common to all trees), with certain parameters containing additional random components, which are specific to individual trees. Note that because the data were limited due to lack of multiple plots, a hierarchical model with grouping of plots and trees within plots was not possible. All combinations of the regression parameters (b_1 , b_2 , and b_3) are candidates for random parameters. Eq. (1) can be written in matrix form as follows:

$$\mathbf{y}_i = \mathbf{f}(\mathbf{b}, \mathbf{u}_i, \mathbf{t}_i) + \varepsilon_i, \tag{2}$$

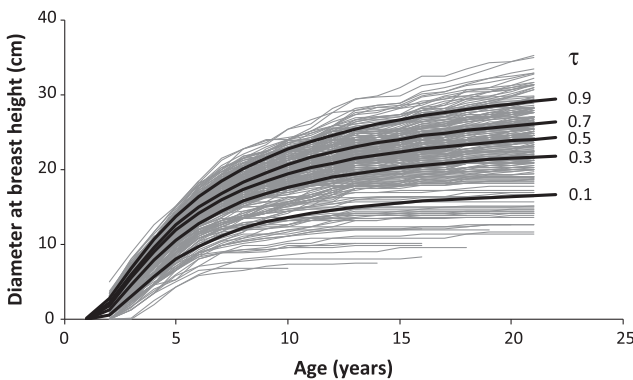


Fig. 1. Graphs of observed tree diameter growth (gray) and curves generated by quantile regressions (black) based on five quantiles.

Table 1
Summary of tree diameters measured at age 21, by group.

Group	N ^a	Mean	SD ^b	Minimum	Maximum
1	50	23.6	4.6	13.0	34.3
2	60	24.4	4.6	14.2	33.0
3	58	23.9	5.3	11.4	35.1
4	53	23.9	4.3	14.2	35.3
5	56	24.4	4.6	12.7	33.5

^a N = number of surviving trees at age 21.

^b SD = standard deviation.

where $\mathbf{y}_i = [y(t_{i1}), y(t_{i2}), \dots, y(t_{i,n_i})]^T$, $\mathbf{t}_i = [t_{i1}, t_{i2}, \dots, t_{i,n_i}]^T$, $\varepsilon_i = [\varepsilon_{i1}, \varepsilon_{i2}, \dots, \varepsilon_{i,n_i}]^T$, n_i is number of measurements for tree i , and \mathbf{b} and \mathbf{u}_i are column vectors of fixed- and random-effects parameters, respectively. The assumptions are:

$$\varepsilon_i \sim N(0, \mathbf{R}), \text{ and}$$

$$\mathbf{u}_i \sim N(0, \mathbf{D}),$$

where \mathbf{R} and \mathbf{D} are diagonal matrices, assuming that the ε_i and \mathbf{u}_i are independent. Procedure NLMIXED from SAS (SAS Institute Inc., 2008) was used to obtain fixed- and random-effects parameters of Eq. (2).

The random parameters \mathbf{u}_i for tree i can be computed by use of the first-order Taylor series expansion (Meng and Huang, 2009):

$$\hat{\mathbf{u}}_i^{k+1} = \hat{\mathbf{D}}\mathbf{Z}_i^T (\mathbf{Z}_i \hat{\mathbf{D}}\mathbf{Z}_i^T + \hat{\mathbf{R}})^{-1} [\mathbf{y}_i - \mathbf{f}(\hat{\mathbf{b}}, \hat{\mathbf{u}}_i^k, \mathbf{t}_i) + \mathbf{Z}_i \hat{\mathbf{u}}_i^k], \tag{3}$$

where $\hat{\mathbf{u}}_i^k$ is estimate of the random parameters for tree i at the k th iteration, $\hat{\mathbf{D}}$ is estimate of \mathbf{D} , the variance–covariance matrix for \mathbf{u}_i , $\mathbf{Z}_i = \frac{\partial \mathbf{f}(\mathbf{b}, \mathbf{u}_i, \mathbf{t}_i)}{\partial \mathbf{u}_i} \Big|_{\hat{\mathbf{b}}, \hat{\mathbf{u}}_i}$, $\hat{\mathbf{R}}$ is estimate of \mathbf{R} , the variance–covariance matrix for ε_i , \mathbf{y}_i is the $m \times 1$ vector of observed diameters, and m is number of measurements used in localizing the diameter growth model. For each growth period, the diameter at the beginning of the period was known, therefore $m = 1$. An iterative procedure was needed to estimate \mathbf{u}_i , whose starting value was set at zero ($\hat{\mathbf{u}}_i^0 = \mathbf{0}$). The value for $\hat{\mathbf{u}}_i$ was then repeatedly updated by means of Eq. (3) until the absolute difference between two successive iterations was smaller than a predetermined tolerance limit. The end result would be the Empirical Best Linear Unbiased Predictor (EBLUP) for random effects.

2.4. Quantile regression model

The same form in Eq. (1) was used to predict the τ th diameter quantile:

$$\hat{y}_\tau(t_{ij}) = \exp(b_1 + b_2 t_{ij}^{b_3}), \tag{4}$$

where $\hat{y}_\tau(t_{ij})$ is predicted value of the τ th quantile of tree diameter at age t_{ij} .

In contrast to the mean regression technique, which employs the least-squares procedure, parameters from the quantile regression are obtained by minimizing

$$S = \sum_{y(t_{ij}) \geq \hat{y}_\tau(t_{ij})} \tau [y(t_{ij}) - \hat{y}_\tau(t_{ij})] + \sum_{y(t_{ij}) < \hat{y}_\tau(t_{ij})} (1 - \tau) [\hat{y}_\tau(t_{ij}) - y(t_{ij})]. \tag{5}$$

A set of q quantile regressions was developed for the fit data, by use of SAS procedure NLP (SAS Institute Inc., 2010). For each diameter measurement in the validation data, the goal was to identify either the quantile regression curve that passed through it, or the two closest quantile regression curves.

If the diameter measurement of tree i at age t_{ij} was encompassed by the m th and $(m + 1)$ st quantile regressions, i.e.

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