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Dipti Dubey, S.K. Neogy

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# Total Dual Integrality and Integral Solutions of the Linear Complementarity Problem

Dipti Dubey\*, S. K. Neogy

*Indian Statistical Institute  
7, S.J.S. Sansanwal Marg  
New Delhi-110016, India*

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## Abstract

This paper deals with the problem of finding an integer solution to a linear complementarity problem (LCP). Chandrasekaran et al. [1] introduced the class **I** of integral matrices for which the corresponding LCP has an integer solution for every integral vector  $q$ , for which it has a solution and proved that for some well known matrix classes principal unimodularity forms a necessary and sufficient condition for inclusion in class **I**. In this paper, we identify some more well-known matrix classes for which principal unimodularity forms a necessary and sufficient condition for inclusion in class **I**. The concept of total dual integrality is utilized to obtain a necessary and sufficient condition for existence of an integer solution to LCP with a **hidden K**-matrix. We interconnect the concept of Hilbert basis with principal unimodularity of a matrix and the corresponding complementary cones. A necessary and sufficient condition is given for the existence of an integer solution of a linear fractional programming problem by using its LCP formulation.

*Keywords:* Linear complementarity problem, Integer solution, Total dual integrality, **Hidden Z**-matrix, Principal unimodularity, Matrix classes.

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\*Corresponding Author

*Email addresses:* diptidubey@isid.ac.in (Dipti Dubey), skn@isid.ac.in (S. K. Neogy)

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