



## ON ZERO SETS IN FOCK SPACES

DRISS AADI, BRAHIM BOUYA, YOUSSEF OMARI

ABSTRACT. We prove that zero sets for distinct Fock spaces are not the same, this is an answer of a question asked by K. Zhu in [6, Page. 209].

## 1. INTRODUCTION AND STATEMENT OF MAIN RESULTS

For  $\alpha > 0$  and  $p > 0$  the Fock space  $\mathcal{F}_\alpha^p$  consists of those entire functions  $f$  satisfying

$$\|f\|_{p,\alpha}^p := \int_{\mathbb{C}} |f(z)|^p dA_{p\alpha/2}(z) < \infty,$$

where

$$dA_\beta(z) := \frac{\beta}{\pi} e^{-\beta|z|^2} dA(z), \quad \beta > 0,$$

and  $A$  represents the Lebesgue area measure on the complex plane  $\mathbb{C}$ . It is known that the space  $\mathcal{F}_\alpha^p$  endowed with the norm  $\|\cdot\|_{p,\alpha}$  is a Banach space when  $p \geq 1$ , while for  $p < 1$  it is a complete metric space, see for instance [6, Chap. 2].

A sequence  $\Lambda$  of complex numbers is called a zero set for  $\mathcal{F}_\alpha^p$  if there exists a function  $f \in \mathcal{F}_\alpha^p \setminus \{0\}$  such that the zero set  $\{z \in \mathbb{C} : f(z) = 0\}$  of  $f$ , counting multiplicities, coincides with  $\Lambda$ . At the present time there is no complete characterization of zero sets for Fock spaces. In [5] and [6, Chap. 5] K. Zhu has presented many properties enjoyed by zero sets in  $\mathcal{F}_\alpha^p$ , in particular he proved that the spaces  $\mathcal{F}_\alpha^p$  and  $\mathcal{F}_\beta^q$  always possess different zero sets in the case where  $\alpha \neq \beta$ , regardless of  $p$  and  $q$ . He then asked whether this remains true if  $\alpha = \beta$ , see [6, Page. 209].

---

*Date:* June 22, 2018.

*2010 Mathematics Subject Classification.* primary 30H20, 30D20; secondary 32C15, 46C99.

Research partially supported by "CNRST" for the third author and by "Hassan II Academy of Science and Technology" for the first and third authors.

Download English Version:

<https://daneshyari.com/en/article/8899235>

Download Persian Version:

<https://daneshyari.com/article/8899235>

[Daneshyari.com](https://daneshyari.com)