## Accepted Manuscript

Completely linear degeneracy for quasilinear hyperbolic systems

Yuzhu Wang, Changhua Wei

 PII:
 S0022-247X(18)30399-8

 DOI:
 https://doi.org/10.1016/j.jmaa.2018.05.006

 Reference:
 YJMAA 22238

To appear in: Journal of Mathematical Analysis and Applications

Received date: 1 February 2018



Please cite this article in press as: Y. Wang, C. Wei, Completely linear degeneracy for quasilinear hyperbolic systems, *J. Math. Anal. Appl.* (2018), https://doi.org/10.1016/j.jmaa.2018.05.006

This is a PDF file of an unedited manuscript that has been accepted for publication. As a service to our customers we are providing this early version of the manuscript. The manuscript will undergo copyediting, typesetting, and review of the resulting proof before it is published in its final form. Please note that during the production process errors may be discovered which could affect the content, and all legal disclaimers that apply to the journal pertain.

# Completely linear degeneracy for quasilinear hyperbolic systems

Yuzhu Wang and Changhua Wei\*

#### Abstract

In this paper, we introduce a new concept of completely linear degeneracy for quasilinear hyperbolic systems in several space variables, and then get an interesting property for multidimensional hyperbolic conservation laws satisfying our new definition. For applications, we give some examples arising from mathematics and physics at last.

### 1 Introduction

Quasilinear hyperbolic systems in several space variables can be described as follows

$$\frac{\partial u}{\partial t} + \sum_{j=1}^{m} A_j(u) \frac{\partial u}{\partial x_j} = 0, \qquad (1.1)$$

where  $u = (u_1, \dots, u_n)^T$  is the unknown vector function of  $(t, x_1, \dots, x_m)$  and  $A_j(u)$   $(j = 1, \dots, m)$  is an  $n \times n$  matrix with smooth elements  $a_{jkl}(u)$   $(k, l = 1, \dots, n)$ . The concepts of linear degeneracy and genuine nonlinearity have been made in the following way (see [24]). This is a straightforward generalization of the case in one space dimension (see [20]). The *i*-th characteristic field of system (1.1) is linearly degenerate, if

$$\nabla \lambda_i(u,\xi) \cdot r_i(u,\xi) \equiv 0, \quad \forall \ u \in \Omega, \ \forall \ \xi \in \mathbb{S}^{m-1};$$
(1.2)

while, it is genuinely nonlinear, if

$$\nabla \lambda_i(u,\xi) \cdot r_i(u,\xi) \neq 0, \quad \forall \ u \in \Omega, \ \forall \ \xi \in \mathbb{S}^{m-1},$$
(1.3)

where  $\xi = (\xi_1, \dots, \xi_m)^T \in \mathbb{S}^{m-1}$ ,  $\lambda_1(u, \xi), \dots, \lambda_n(u, \xi)$  are *n* real eigenvalues of  $A(u, \xi) = \sum_{j=1}^m A_j(u)\xi_j$  and  $\{r_i(u,\xi)\}_{i=1}^n$  is a complete set of right eigenvectors of  $A(u,\xi)$ . Here and throughout this paper, we always assume that  $A(u,\xi)$  has *n* real eigenvalues. However, as is pointed out in [21], this generalization would exclude a single equation and a system of two

<sup>\*</sup>Corresponding author: changhuawei1986@gmail.com.

<sup>2000</sup> Mathematics Subject Classification: 35L40, 35L65.

Key words and phrases: Quasilinear hyperbolic systems, completely linear degeneracy.

Download English Version:

# https://daneshyari.com/en/article/8899504

Download Persian Version:

https://daneshyari.com/article/8899504

Daneshyari.com