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## Effect of cross-diffusion in the diffusion prey-predator model with a protection zone II \*

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Abstract–In the current paper, we continue the mathematical analysis studied in [S. Li et al., Discrete Contin. Dynam. Syst. 37 (2017) 411-430, K. Oeda, J. Differential Equations 250 (2011) 3988-4009], and further study the effect of cross-diffusion for the predator on the stationary problem. The existence of positive solutions is first established by the bifurcation theory. We next discuss the limiting behavior of positive solutions when the intrinsic growth rate of the predator species tends to infinity. Moreover, as the prevention coefficient tends to infinity, we obtain two shadow systems and give the complete limiting characterization of positive solutions.

**Keywords**–Cross-diffusion, Protection zone, Coexistence solution, Limiting behavior, Shadow system.

**MSC**-35J65, 35B32, 35B35, 92D25.

## 1 Introduction

This paper is devoted to studying the following prey-predator model with a protection zone and nonlinear diffusions:

$$\begin{aligned} & u_t = \Delta[(1+k\rho(x)v)u] + u(\lambda - u - b(x)v), \quad (x,t) \in \Omega \times (0,\infty), \\ & v_t = \Delta\left[\left(1 + \frac{\alpha}{1+\beta u}\right)v\right] + v(\mu - v + cu), \qquad (x,t) \in \Omega \setminus \overline{\Omega}_0 \times (0,\infty), \\ & \partial_n u = 0, \qquad \qquad (x,t) \in \partial\Omega \times (0,\infty), \\ & \partial_n v = 0, \qquad \qquad (x,t) \in \partial \left(\Omega \setminus \overline{\Omega}_0\right) \times (0,\infty), \\ & u(x,0) = u_0(x) \ge 0, \qquad \qquad x \in \Omega, \\ & v(x,0) = v_0(x) \ge 0, \qquad \qquad x \in \Omega \setminus \overline{\Omega}_0, \end{aligned}$$
(1.1)

where  $\Omega$  is a bounded domain in  $\mathbb{R}^N$  with smooth boundary  $\partial\Omega$ ,  $\Omega_0$  is a subdomain of  $\Omega$  with smooth boundary  $\partial\Omega_0$  such that  $\overline{\Omega}_0 \subset \Omega$ , the parameters  $k, \alpha, \beta, \lambda, \mu, c$  are constants with  $\lambda, c$ positive and  $k, \alpha, \beta$  nonnegative,  $\mu$  may change sign, b(x) and  $\rho(x)$  are smooth functions in  $\overline{\Omega}$  with  $\rho(x) = b(x) = 0$  in  $\Omega_0$  and  $\rho(x) > 0$  and b(x) > 0 in  $\Omega \setminus \overline{\Omega}_0$ . For more details on the protection zone see references [3,8–11,15,17,22,23,25] and references therein. For more details on the cross-diffusion see references [2,5,12–14,16,19–21,26,29] and references therein.

In (1.1), when cross-diffusion is absent, i.e.,  $k = \alpha = 0$ , Du et al. have studied the effects of protection zone for the prey on Holling type II prey-predator model [8], and they have obtained

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