



Zipf distribution in top Chinese firms and an economic explanation

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ABSTRACT

By analyzing the data of top 500 Chinese firms from the year 2002 to 2007, we reveal that their revenues and ranks obey the Zipf's law with exponent of 1 for each year. This result confirms the universality of firm size character which has been presented in many other empirical works, since China possesses a unique ideological and political system. We offer an explanation of it based on a simple economic model which takes production and capital accumulation into account.

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1. Introduction

Firms or enterprises, responsible for carrying out economic activities by providing various products and services, play key roles in countries. Firm size can be measured by a number of quantities: revenue, asset, employee or profit and so on. It is often used to represent firm's competition capability in the economy. Firm size varies enormously, from the sole trader up to a huge corporation employing thousands of people. For instance, *Wal-Mart Stores*, according to *Fortune* magazine of May 5th, 2008, ranked 1st in the top 500 American corporations list again for its amazing size. The value of its asset, revenue and profit is respectively 163,514 million, 378,799 million and 12,731 million dollars. The size distribution of firms in many countries was found to be likely consistent—it is highly skew, the small firms are extremely common, whereas large ones are extremely rare [1]. This topic has been attractive all along, especially in testifying its validity in various economies and seeking theoretical explanations.

As a pioneering study on the size distribution of firms, Gibrat reported that firm size could be described by lognormal distribution [2]. The same distribution was discovered in some followed empirical studies [3–6]. However, other empirical studies show that the size distribution (especially at upper tail) can be approximated closely by the Pareto or power-law distribution in the form of $P(X > x) \sim x^{-k}$ [7–9]. Inspired by the well-known work of Zipf [10], who firstly found that assets of US corporations follow Zipf's law: $S(r) \sim r^{-\beta}$, where $S(r)$ is the size of the corporation ranked r in a list ordered by asset size, beginning with the largest, great interest was attracted in the relationship of sizes and their corresponding ranks, and many considerable evidences on Zipf distribution of firm size were discovered later [11–14]. Actually, Zipf's law is consistent with Pareto or power-law distribution, they are different representations of the same fact. The relation of their exponents can be given by $\beta = 1/k$ [15].

Regarding the mechanisms behind this universal distribution, the most elementary firm dynamic model is that in Ref. [2], where Gibrat presented the law of proportionate growth to explain the lognormal distribution. However, by assuming

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some version of a reflective lower bound, models of proportionate growth were widely applied to generate Pareto upper tail in economics [7,16–18]. Since firm size distribution provides another evidence of the universality of Zipf's law, the dynamics of firms gradually attracted the interests of physicists, especially those who work in econophysics [19–23]. Axtell insisted on using complexity approach to deal with the problem, and believed that agent-based modeling together with evolutionary dynamics should be helpful to understand the formation of power law [19]. Malcai et al. combined a random multiplicative dynamics at the individual level with a global coupling through a constraint given by the average of the agents' values to produce the power-law distribution [20]. Ree proposed an additive preferential rule to generate the power-law distribution [21]. Wang et al. constructed a bipartite producer-consumer network to explain the power-law distribution in firm size [22]. Reed and Hughes showed that if stochastic processes with exponential growth in expectation were killed randomly, it led to power-law tails in statistical distributions [23].

As listed above, many intriguing results have been achieved on firm size distribution, but there are still two aspects needing to be concerned further. Firstly, in contrast to these numerous works on developed economies, only a few researches have been carried out on developing countries [24]. Since some studies have indicated that company size distributions are not universal but clearly depend on countries [9,25]. It is very necessary to further widen the scope of this research. China, the biggest developing country in the world, attracted the eyes of the world for its market economy reform and sustaining high economic growth. Chinese companies have grown bigger and get more power in worldwide economic activities. For instance, *Sinopec* ranked 17th in *Fortune Global 500* of the year 2007, which only ranked 86th in 2002. For another example, *Lenovo*, has acquired *IBM*'s entire global desktop and notebook computer business, and gradually plays more and more important roles in world personal computer market these years. It is meaningful to check whether the Zipf's law holds up in such a unique ideological and political system. Secondly, although many theoretical models have been introduced to explain Zipf's law in firm size, most of them only use simple stochastic or physical mechanisms without sufficient economic senses. They ignore the real mechanism of economic operation and cannot give us any practical advices on the firm's real dynamics.

In this paper, we show the character of Chinese firms and try to give an economic explanation. The remainder is organized as follows: Section 2 carefully checks the data and displays the upper tail distribution of firms' sizes in China from the year 2002 to 2007. Section 3 has some discussions on it from the view of economics and in Section 4 we conclude.

2. The data and the distribution

The datasets used in this paper were published in series volumes of “*A Report on the Development of China's Enterprises*”. They are provided annually by the organization named *China Enterprise Confederation* since the year 2002. The data consist of some basic information of top 500 Chinese enterprises ranked in revenue scale, including the firms' names, their revenues and corresponding ranks. Till now, six years' data are available.

It is very clear that the list of top 500 enterprises is changing, the revenue and corresponding rank for the same firm also fluctuate all the time. For example, *China National Heavy Duty Truck Group Corp.*, its revenue is respectively 5.159, 10.231, 15.124, 23.389, 14.394, 13.263 billion RMB, and its rank is 214, 143, 124, 107, 216, 289 from the year 2002 to 2007. Further more, we also find out (I) revenues of firms are mostly below 200 billion RMB, only a few firms are of great revenues while small firms are extremely common; (II) there is a big gap of revenue between the 1st firm and the 500th one, for instance, in 2007 the revenue of the 1st firm reaches 1064.667 billion RMB while that of the 500th only amounts to 7.216 billion RMB; (III) the gap between two contiguous firms ranking upper is much larger. As an example, the gaps between the 1st and 2nd, 249th and 250th, 499th and 500th are respectively 56 733.550, 40.150, 5.420 million RMB in the year 2002.

Fig. 1 shows the relation between revenues and their ranks of these firms in double logarithmic scale. Almost all of these curves parallel with the dashed straight lines with a slope of -1 . As a result, the revenues of the top companies in China could be primarily concluded to exhibit Zipf's law. To get the precise Zipf's exponent, we use the fitting technique proposed by Gabaix et al. [26], which is a modified OLS estimation as below:

$$\log(S) = \alpha - \beta \log(r - 0.5), \quad (1)$$

where S is the firm size, r is its rank, and β is the Zipf's exponent needing to be estimated. This estimating can reduce the bias and performs well in the case of small samples where OLS procedure is strongly biased. The true standard error here, not the OLS standard error, is asymptotically $\sqrt{\frac{2}{n}}\beta$, where n is the number of samples.

In this case, the estimate and test are carried out by choosing segments in the rank list from 20 to 500 for all these six years. The results of estimate are listed in Table 1, including the estimates of exponent ($\hat{\beta}$), their corresponding determination coefficients (R^2) of these regression equations and the standard deviations (σ) defined above. It is shown that the exponent estimates of the six years are all around 1. Then we use the Kolmogorov–Smirnov (KS) statistics [27] to confirm the fitness of our result. The KS statistic is simply the maximum distance between the cumulative distribution functions (CDF) of the data and that of the fitted model:

$$D = \max_{x \in R} |F(x) - P(x)|, \quad (2)$$

where $F(x)$ denotes the empirical CDF and $P(x)$ is the hypothesized CDF. As listed in Table 1, the KS statistics are all less than 0.04. These results indicate that it is insufficient to reject the conclusion that the revenues of the samples follow a Zipf distribution.

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